

Momentum Compensation for the Fast Dynamic Walk of Humanoids based on the Pelvic Rotation of Contact Sport Athletes

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This paper presents a method of momentum compensation around the perpendicular axis of the stance foot during fast dynamic walk of humanoid robots. In order to perform a task using the arms during a walk, it is desirable that the upper body part, i.e., the arms and the trunk, should not be used for the momentum compensation and should be dedicated to achieving a task. Moreover, a particular walk called a trunk-twistless walk is investigated by experientially observing the pelvic rotation of contact sport athletes. From these observations, an antiphase rotation of the pelvis against the swing leg is observed when compared to the normal walk of a human. This antiphase characteristic of the pelvic rotation is implemented to a humanoid. A method of determining the rotation of the humanoid's waist is proposed in conjunction with the pitch angle of the swing legs. The proposed walk achieves a whole walking motion including momentum compensation only by the lower body. The stance foot torque around the perpendicular axis is reduced in the proposed walk compared to a standard humanoid walk without twisting the trunk or swinging the arms. Improvements to the straightness of the walking trajectory and the stability of the upper body during a fast dynamic walk are also confirmed.

Keywords: Humanoid robot, Biped walking, Momentum compensation, Trunk-twisting, Athlete, Friction, Motion capture

1. Introduction

Biped walking for humanoid robots has almost been achieved through ZMP theory¹²³. Recently, the research on humanoids has begun to focus on achieving tasks using the arms during walking, in tasks, such as carrying a load (for example, a heavy backpack) or interacting with environments⁴. In order to achieve a stable biped-walking, the momentum around the perpendicular axis generated by the swing leg must be counterbalanced. If this momentum exceeds the maximum static friction torque between the floor and the stance foot, the body will begin to slip and rotate around the perpendicular axis. In a normal human walk, the upper body compensates this momentum, i.e., by rotating the thorax (or shoulders) and swinging the arms in an antiphase of the swing leg⁵⁶⁷. For humanoid control, research has been presented for momentum compensation using the motion of the entire body including the arms⁸⁹¹⁰¹¹. However, momentum compensation by the upper body is undesirable for a humanoid that uses its arms to achieve a task since this type of compensation limits the degree of freedom (DOF) for the task. In addition, the fluctuation of the upper body has a bad effect not only on the task accomplishment, but also on visual processing since most vision systems are attached to the head part. As a result, it is desirable to preserve as many degrees of freedom of the upper body as possible, and to suppress the fluctuation of the body at the same time. The walking action including momentum compensation should be completed only by the lower body, which leads to a simplification of motion planning.

Improving the performance of humanoids through observations of humans walk seems natural. Recently, however, in the field of exercise and sports science, a clarification of efficient motion in the human has begun, and this clarification has been accompanied by improvements in the measuring equipments used for this endeavor. Many common features can be observed in the motion of contact sport athletes, i.e., they move so as not to twist their trunks as much as possible. This kind of trunk-twistless walk is better understood than before, but is considered inefficient since the walking pattern in the trunk-twistless walk is different from normal one¹²¹³. However, a decreased pelvic and thoracic rotation, similar to trunk-twistless walk, has been observed with a load carriage⁷. This decrease in pelvic and thoracic rotation indicates that not twisting the trunk and not swinging the arms, but other momentum compensation, is performed when the intensity of upper-body exercise is high. Therefore, this trunk-twistless walk may be helpful to humanoids for achieving tasks; however, the characteristic of this walk has not been clarified, and its result has not been applied to humanoids.

In this paper, the characteristics of the trunk-twistless walk are quantitatively investigated from the observation of contact sport athletes. The relative phase of the swing leg and the pelvic rotation appears to be in an antiphase when compared with the normal walk of humans. This leads to the possibility of momentum compensation by pelvic rotation, and this characteristic of the pelvic rotation is implemented to a humanoid in experiments conducted in this paper. A method of determining the rotation of the humanoid's waist is proposed in conjunction with the pitch angle of the swing legs. In this paper we confirm that the torque around the perpendicular axis is reduced in the humanoid trunk-twistless walk when compared to a standard humanoid walk without the twisting of the trunk or swinging of the arms. Improvements on the straightness of the walking trajectory and on the reduction in the fluctuation of the upper body during a fast dynamic walk are also confirmed.

2. Walking Measurement

2.1. *Methods and Subjects*

Three healthy male subjects who are accustomed to the trunk-twistless walk served as subjects. All subjects are contact sport athletes of rugby football, karate, and kendo (the Japanese art of fencing) respectively. All subjects have been coaches. Their mean age, body height, and body weight were 42.6 ± 7.0 years (mean \pm S.D.), 171.33 ± 1.52 cm, and 79.3 ± 6.02 kg. Subjects were given several minutes to get used to treadmill walking. The treadmill velocity was set to 1.5 km/h, 3.0 km/h and 4.0 km/h. The normal walk and the trunk-twistless walk were measured for 30 seconds.

A motion capture system with twelve cameras (Vicon Motion Systems Ltd.) was used to measure three dimensional kinematic data (sampling frequency 120Hz) from the reflective markers shown in Fig.1(a). Two 3-axis accelerometers were attached on both iliac crests to measure the antero-posterior and medio-lateral accelerations of the pelvis. The twisting angle of the trunk was measured using the four markers shown in Fig.1(b). The thoracic and pelvic rotation around the perpendicular axis, θ_{thorax} and θ_{pelvis} in Fig.2, are measured by the markers on both clavicles and both iliac crests respectively. Both angles are set to 0 when the subject is exactly facing the forward direction. The yaw-axis torque exertion from the stance foot to the

floor is defined as τ_{LF} and τ_{RF} for each foot^a. When τ_{LF} increases to positive and exceeds the maximum static friction, the body begins to rotate clockwise due to the slip that occurs at the stance foot.

After walking on the treadmill, the subjects were asked to walk on the pressure distribution sensor (Big-Mat, Nitta Corporation, 440mm × 1920mm) to measure the trajectory of the COP(Center of Pressure) of the stance foot.

2.2. Comparison of Trunk Twisting and Pelvic Rotation

Fig.4 shows typical examples of the captured walking posture in one walking cycle from behind of the subject. In this figure, the postures at LC(Left heel Contact), RO(Right toe OFF), RC(Right heel Contact), LO(Left toe OFF), and next LC are shown.

From Fig.4, it is observed that the step width of the athlete’s walk is wider

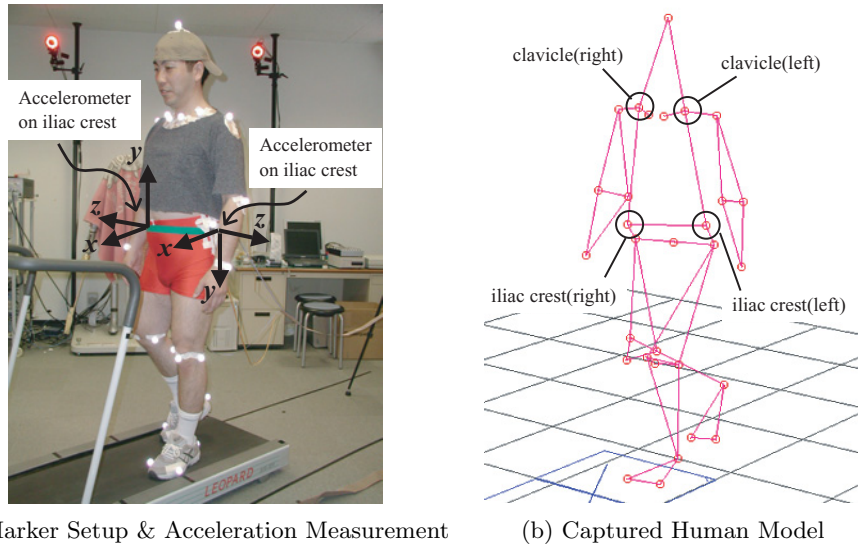


Fig. 1. 3-D Motion Capture

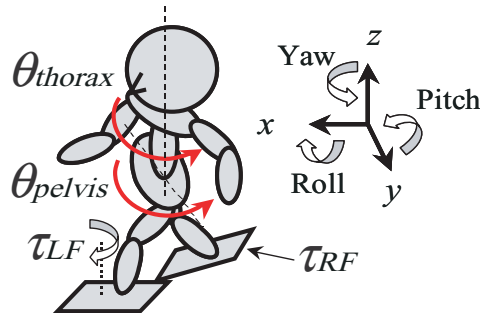


Fig. 2. Pelvis-thorax Rotating Angle and Yaw Moment of Stance Foot

^aThe foot rotation around the perpendicular axis is the main focus of this paper. Whenever context permits, we use torque/momentum to the torque around the perpendicular/yaw axis.

than the normal walk, and the posture of the stance feet is in external rotation. In addition, the amplitude of pelvic rotation is small, and the relative phase between the swing leg and the pelvis is different compared to the normal walk.

The twisting angle of trunk θ_{twist} is obtained by subtracting θ_{pelvis} from θ_{thorax} :

$$\theta_{twist} = \theta_{pelvis} - \theta_{thorax} \quad (1)$$

Fig.5 shows the typical thorax, pelvis, and twisting angles at 4.0 km/h. The bottom graph shows the stance phase, LC and RC. In the trunk-twistless walk, the relative phase between the pelvic and thoracic rotation is smaller, resulting in a smaller twisting angle of trunk than in the normal walk. In comparison to the stance phase, the relative phase between the leg and the thorax is almost the same for both types of walking, but the difference can be found in the pelvic rotation.

The counterclockwise rotation of the pelvis is observed for the normal walk when the right leg is in the air, whereas in the trunk-twistless walk, the clockwise rotation is observed in the same period. As a result, the relative phase of the swing leg and the pelvic rotation can be said to be in an antiphase for the trunk-twistless walk compared to the normal walk.

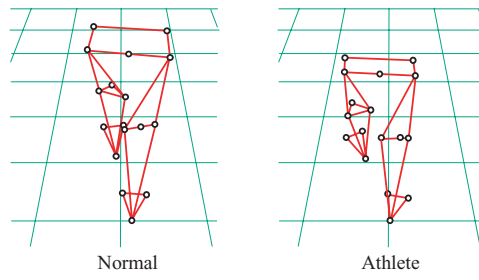
Fig.6 shows the walking velocity versus the relative phase of the thoracic and pelvic rotation. For all walking velocities, the relative phase of the trunk-twistless walk is smaller than the normal walk. The relative phase increases when the walking velocity increases as reported in conventional researches⁶⁷; however the tendency is the same.

2.3. *Yaw-axis Torque between Stance Foot and Floor*

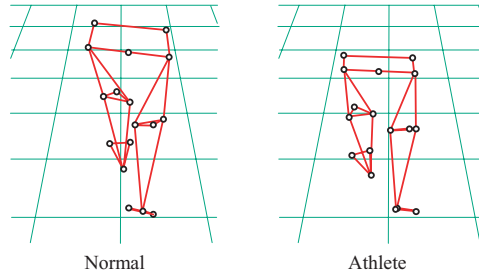
Fig.7 shows the trajectories of the COP(Center of Pressure). Similar to Fig.4, the step width of the trunk-twistless walk is wider than the normal walk, and the posture of the stance feet is in external rotation. Fig.8 shows the transition of the pressure distribution of left stance foot for every 10ms from LC to LO. As shown in Fig.8(a) of the normal walk, the COP moves relatively straight from the heel, thenar eminence, then the first toe. In contrast, the COP moves from the heel, hypothenar eminence, and then the thenar eminence like a curve in the trunk-twistless walk. Note that the first toe is off without being pressured in this case. This difference



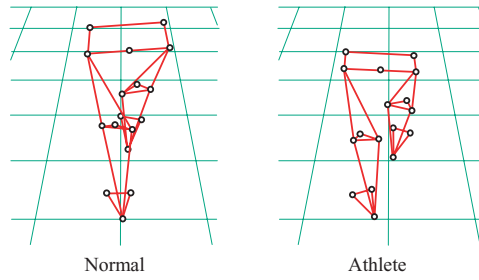
Fig. 3. Pressure Distribution Measurement of Stance Foot



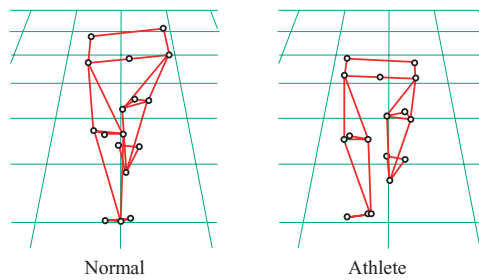
(a) LC



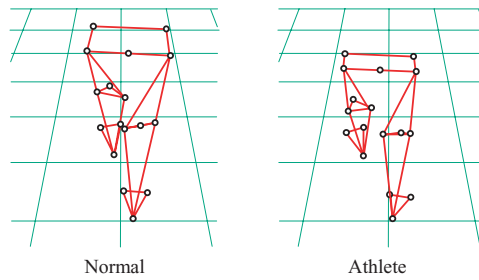
(b) RO



(c) RC



(d) LO

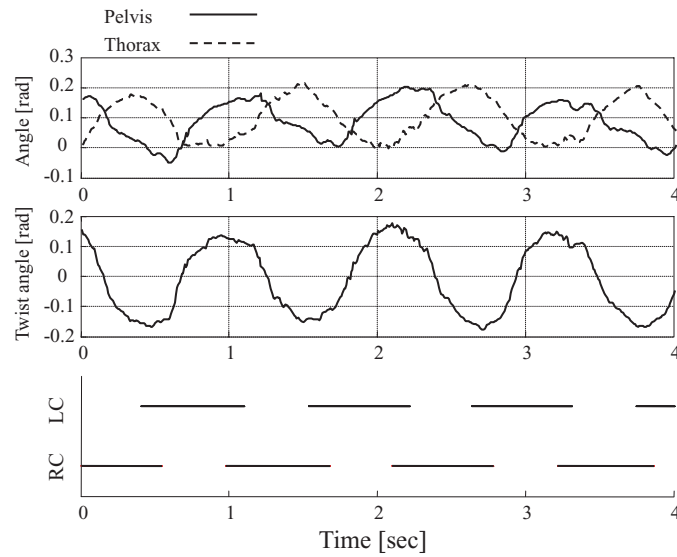


(e) Next LC

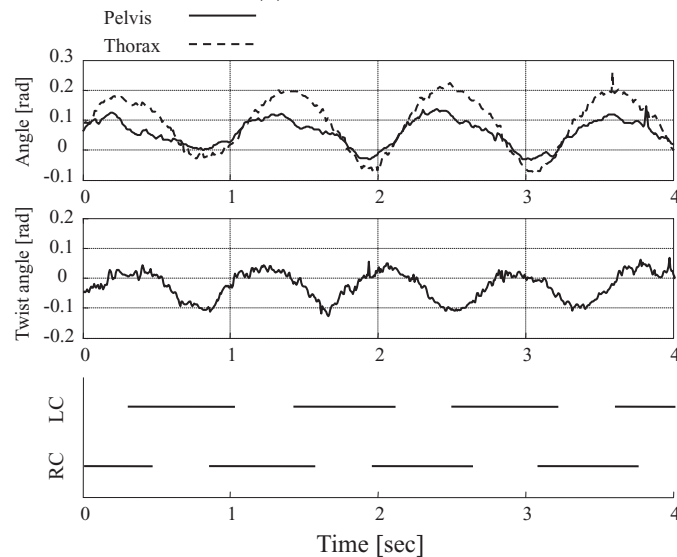
Fig. 4. Captured Walking Motion (from behind)

between the COP trajectories can also be observed in Fig.9(COP trajectories within the left stance foot).

In order to clarify the reason for this curved COP trajectory, a preliminary experiment was performed. First, a subject stands only on his left foot on the pressure distribution sensor. Next, the subject externally rotates the left hip joint so as to rotate the body clockwise by 90 degrees. At this moment, a counterclockwise torque must be applied to the stance foot due to the body's rotation. Fig.10 shows the measurement result during the process, in which a similarity to Fig.8(b) is observed. This result indicates that the curved COP trajectory occurs when a torque is applied from the stance foot to the floor.



(a) Normal Walk



(b) Trunk-twistless Walk

Fig. 5. Twisting Angle of Trunk

2.4. Discussion of Momentum Compensation of the Trunk-twistless Walk

The trunk-twistless walk was quantitatively investigated from the observation of contact sport athletes. The typical characteristics in comparison with the normal walk are:

- (1) Externally rotated posture of the stance feet.
- (2) Wide stance width.
- (3) Small relative phase between the pelvic and thoracic rotation (Small trunk twisting).
- (4) Curved COP trajectory (Torque transmission at the stance foot).
- (5) Antiphase of the swing leg and the pelvic rotation.

In a normal human walk, the momentum is compensated by the upper body, i.e., by rotating the thorax (or shoulder) and swinging the arms in antiphase of the swing leg. This motion leads to canceling the torque at the stance foot and avoiding the rotational slip. However, in contact sports, the upper-body posture should be maintained to the front as much as possible in preparation for contacting

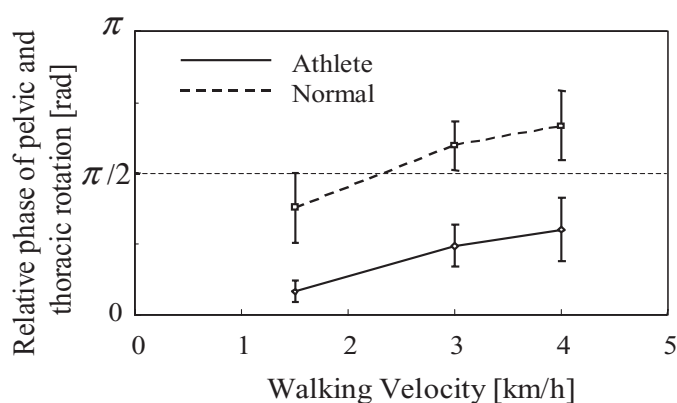
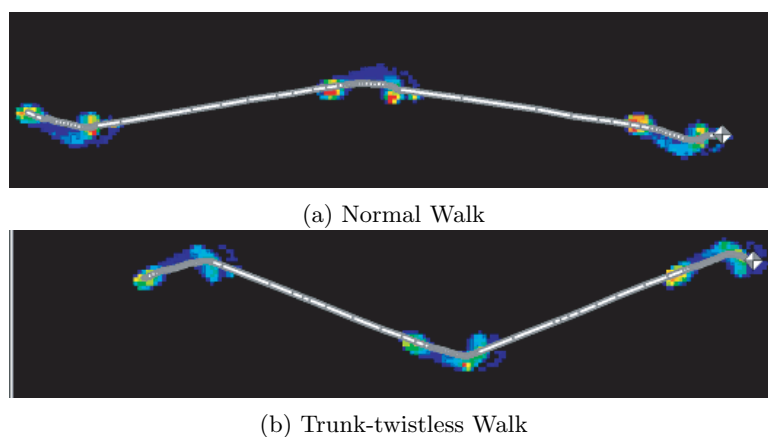


Fig. 6. Comparison of Twisting Angle of Trunk (average of 3 subjects)



(b) Trunk-twistless Walk

Fig. 7. Trajectory of COP

against the environments. A similar phenomenon can be observed when the contact increases the intensity of the upper-body exercise. It is assumed that the contact sport athletes perform the trunk-twistless motion for the upper-body exercise. A decreased pelvic and thoracic rotation, similar to the above case, has been observed with a load carriage (carrying a heavy backpack)⁷. Without twisting the trunk or swinging the arms, the momentum should be compensated by other methods. Our hypothesis is that the momentum is simultaneously compensated passively by the friction at the stance foot and actively by the antiphase pelvic rotation.

First, we discuss the passive compensation caused by the friction. The externally rotated posture of the stance feet and the COP trajectory without passing toes are necessary for the transmission of the torque generated by the hip joints. We have reported that the toes (especially the big and 2nd toes) are important for balance of the upper body¹⁴. It is assumed the step width becomes wider for the balance. In addition, the translational force at the stance foot can cancel the momentum when the step width becomes wide.

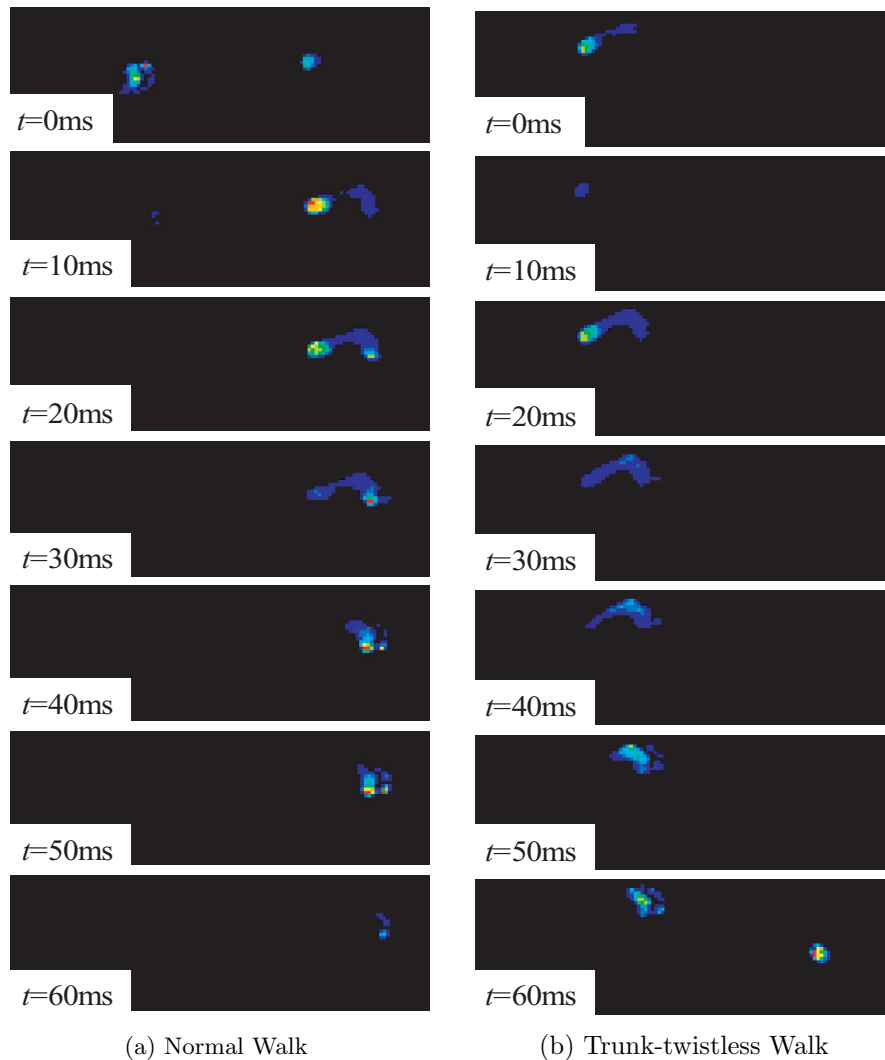


Fig. 8. Comparison of Pressure Distribution of Stance Foot

Next, active compensation by the antiphase pelvic rotation is discussed. In Fig.2, τ_{LF} increases when the right leg is accelerated and swung forward in the initial part of left leg stance phase. In the normal walk where the leg and the pelvis are in-phase, the momentum due to the increase of θ_{pelvis} also increases τ_{LF} . In this case, the sum of the momentum should be compensated by trunk twisting and arm swinging. On the other hand, in the trunk-twistless walk where the leg and the pelvis are in an antiphase, the decrease of θ_{pelvis} cancels τ_{LF} . Also, the momentum of inertia of the pelvis is not large when compared to the momentum of inertia of the legs; in other words, the total momentum is not compensated by this active pelvic rotation only. However, the twisting action of the trunk seems unnecessary when combined with passive compensation. In this paper, we focus on this antiphase pelvic rotation, and apply this antiphase rotation to fast walking by humanoids.

3. Moment Compensation for Humanoids using Waist Rotation

3.1. Humanoid Robot: HRP-2

Fig.11 shows the overview and the actuator configuration of the humanoid HRP-2¹⁵ used in this paper. Its height is 154cm and weight is 58kg, which are close the height and weight of a human. HRP-2 has 30 DOF in total. One characteristic of the HRP-2 is a joint around the perpendicular axis between the chest and the waist. Along with the hip joints, the chest part and the waist part rotate independently around the perpendicular axis as shown in Fig.11(a). The pelvic rotation discussed in section 2 can be implemented to HRP-2 by correlating the robot's waist to a human's pelvis and its chest to a human's thorax. A simulation software, OpenHRP¹⁶, is also available. In this paper, both experiment and simulation are performed for the investigation, but a very fast walk, which cannot be realized by the real hardware, is examined only in the simulator.

3.2. From Athlete Measurements to Humanoids

In section 2, the antiphase pelvic rotation was observed in the trunk-twistless walk of contact sport athletes. The advantages of the application to humanoids are as

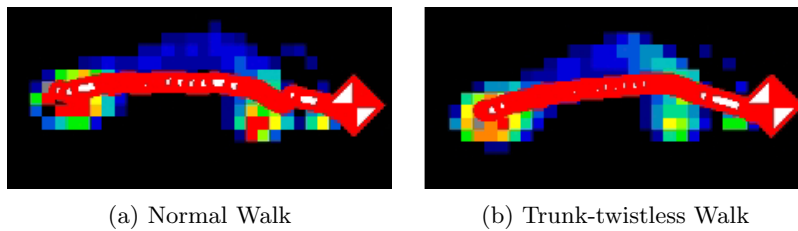


Fig. 9. Trajectory of COP of Stance Foot

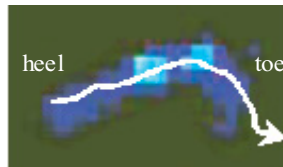


Fig. 10. Trajectory of COP when exerting Yaw-axis Moment

follows:

One goal of the research on humanoids is to achieve a task where the humanoid carries a load or interacts with environments⁴ using its upper body. The use of the upper body for walking itself, however, is undesirable for this purpose. The walking action including momentum compensation should be completed only by the lower body in order to preserve the freedom of the upper body.

In general, humanoids have larger feet for static stability, hence the maximum friction torque of the sole is larger than the human's. The rotational slip was not generated without considering the momentum in a low-speed walking pattern; however, this slip becomes a problem when the walking velocity is increased. In this case, the trunk-twistless walk preserves the upper body's DOF by waist rotation. As a secondary effect, the trunk-twistless walk provides the humanoids with an easy visual processing using a vision system attached to the head part.

As shown in Fig.7(a) in the walk of normal humans, the feet contact the floor more closely to the center of the body, resulting in a step width narrower than the shoulder. However, in recent version of the humanoid's walk, the feet move in parallel to the walking direction, thus resulting in the same step width of the shoulders³. This result merely comes from a simplification of the walking pattern and a collision avoidance pattern between the feet. On the other hand, the expansion of the step length in the trunk-twistless walk is related to balance maintenance and torque transmission. Although humanoids are not alive and athletes are very much so, both can perform the same walk with the same wide step width, which leads to easiness of implementation in the measurement result.

3.3. Evaluation of Humanoid Walk

The walking pattern with swinging arms and twisting trunk, which is common to the majority of people, cannot be regarded as a humanoid's standard walk. In this paper, we apply the antiphase pelvic rotation of athletes to humanoids. First, the standard walk of a humanoid is defined as shown in Table 1 to make clear the effects on momentum compensation without using the upper body. Note that we

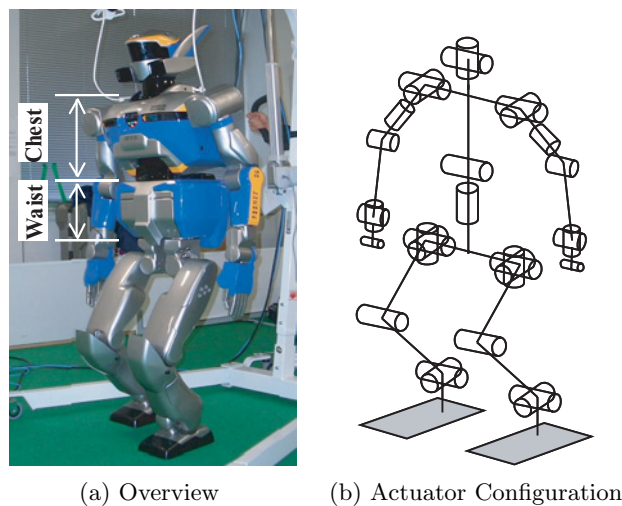


Fig. 11. Humanoid HRP-2

use ‘standard’ for a humanoid walk to distinguish this walk from the ‘normal’ walk of humans. In the standard walk of a humanoid, the upper body (above the chest) is not twisted and is planned to facing the forward direction. The swinging arms is not performed; therefore, the walking action is completed only by the lower body.

The waist rotation is set in-phase of the swing leg for the humanoid’s standard walk, the same as in a human’s normal walk. In contrast, the antiphase rotation of the waist is performed for the proposed walk of the humanoid, and is obtained by (2) presented in the following section. In addition, in the middle of the standard and the proposed walk of the humanoid, the waist-fixed walk is defined without the waist rotation. The step width is set equal to the shoulder’s width for all patterns by applying the result of the step width, which allows us to use a standard pattern generator³. Note that all three patterns have the same trajectory, velocity, posture, and landing positions for the foot in the air by using the redundancy of the waist and leg part. As a result, the walking velocity, step length, and step width are the same. The only difference is the waist rotation.

3.4. Momentum Compensation by Waist Rotation

Fig.12 shows the total left stance foot torque and the component generated by the right swing leg. As is observed in the graph, the component of the swing leg occupies a large percentage of the total momentum. In order to effectively cancel the stance foot torque by the waist rotation, the waist should be counterbalanced to the largest factor, i.e., the leg motion. The angle of the waist rotation is obtained as follows coupling with the pitch angle of the hip joints:

$$\theta_{pelvis} = k \frac{\theta_R(t) - \theta_L(t)}{\theta_{max}} \quad (2)$$

where $k=0.175[\text{rad}](10.0[\text{deg}])$ is the maximum amplitude of the waist rotation used to obtain the same amplitude of the standard walk. $\theta_R(t)$ and $\theta_L(t)$ are pitch angles of both swing legs shown in Fig.13, $\theta_{max}=0.5[\text{rad}](28.6[\text{deg}])$ is the maximum of $(\theta_R(t) - \theta_L(t))$ in one walking cycle. By using (2), the antiphase rotation is generated for the proposed walk compared with the standard walk as shown in Fig.14. The stance foot torque due to the acceleration of the swing leg is canceled by the waist angular momentum.

4. Fast Dynamic Walking of Humanoid

4.1. Comparison of Stance Foot Torque

The effect of the waist rotation for reducing the stance foot torque is confirmed both by simulation and experiment. Fig.15 shows the body posture at 0.83km/h.

Table 1. Humanoid’s Walk

	Standard	Waist fixed	Propose
Waist rotation & leg swing	In-phase	0	Antiphase (Eq. (2))
Arm swing	0	←	←
Chest Rotation	0	←	←
Step width	Shoulder width	←	←

As shown in the experiment, the body posture for both types of walking is the same except the waist rotation. The antiphase waist rotation is realized in the proposed walk. Fig.16 shows the left stance foot torque by the standard, the waist-fixed, and the proposed walk respectively.

As shown in Fig.16(a) on the simulation, the torque is decreased by 30% compared with the waist-fixed walk, and by 37% from the standard walk. As shown in Fig.16(b) on the experiment, the torque is decreased by 30% from the standard one. The validity of the proposed walk can be confirmed in both cases. The difference of the wave form between the simulation and the experiment is due to several unavoidable problems with the experiments, e.g., control delay and modeling errors of the robot itself as well as the impact. Fig.17 shows the RMS (Root Mean Square) of the stance foot torque. The validity can be observed not only in the peak torque but also in the average torque.

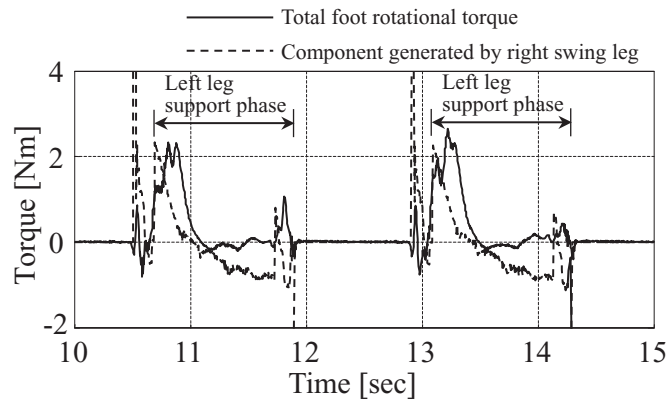


Fig. 12. Component of Stance Foot Torque (Simulation, 0.83km/h)

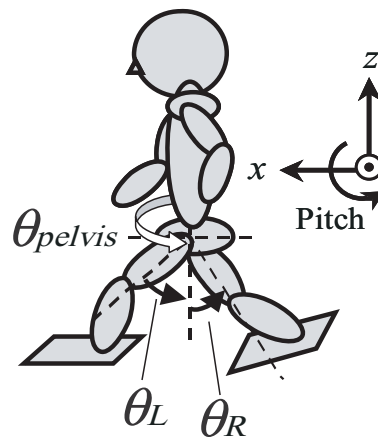


Fig. 13. Rotation Angle of Waist and Pitch Angle of Swing Leg

4.2. Improvement of Straightness and Upper-body Stability

From a safety perspective, it was difficult for the humanoid to walk fast without slipping at a speed exceeding 1.0 km/h. The following investigations were performed by the simulation: Fig.18 shows the relation between the peak torque and the walking velocity. This relation indicates that a faster walk without slipping can be achieved by the proposed walk for a floor with the same friction coefficient. For example,

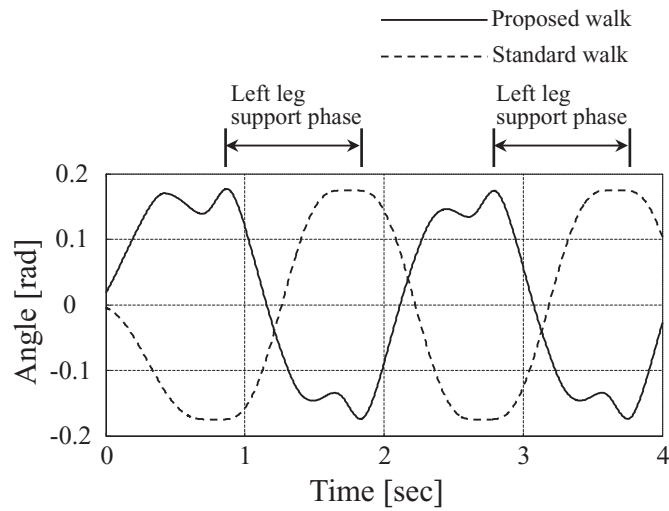
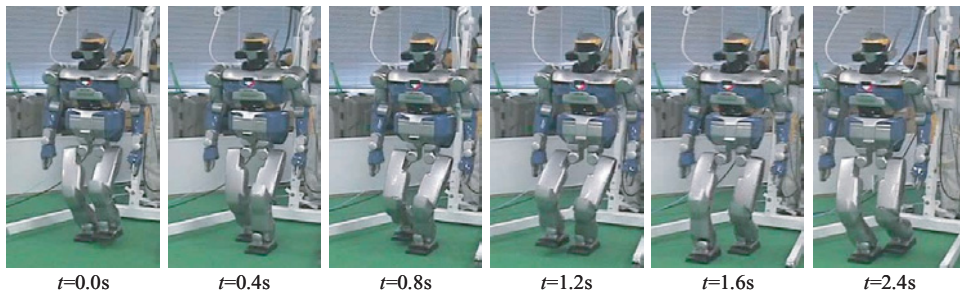
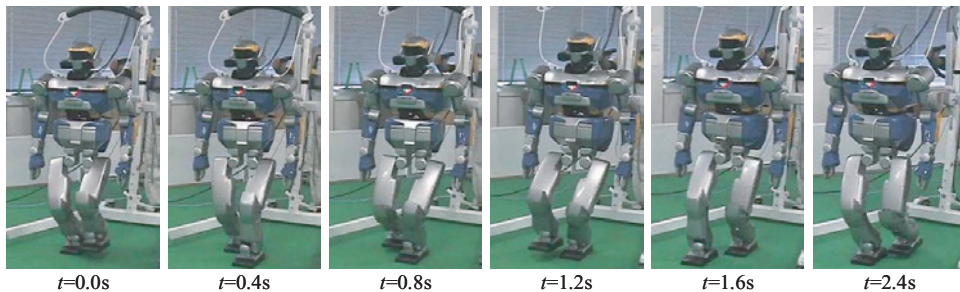


Fig. 14. Rotation Angle of Waist (Simulation, 0.83km/h)



(a) Standard Walk (In-phase waist rotation)



(b) Proposed Walk (Antiphase waist rotation)

Fig. 15. Experiments with Humanoid (0.83km/h)

the peak torque is 9.4Nm at 2.5km/h by the standard walk, whereas it is 9.6Nm

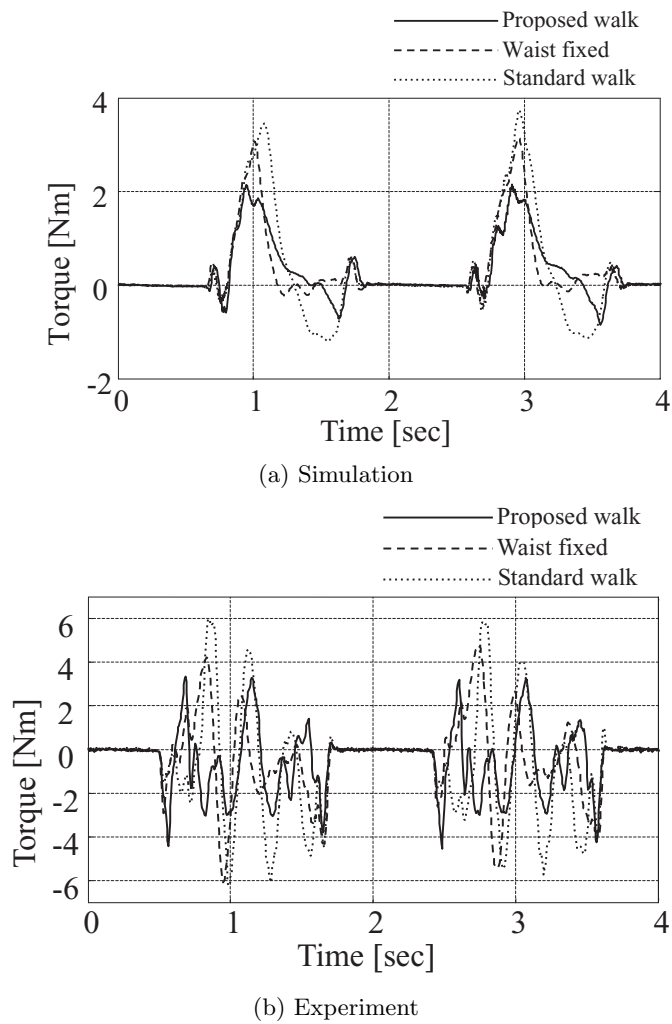


Fig. 16. Yaw-axis Torque of Stance Foot (0.83km/h)

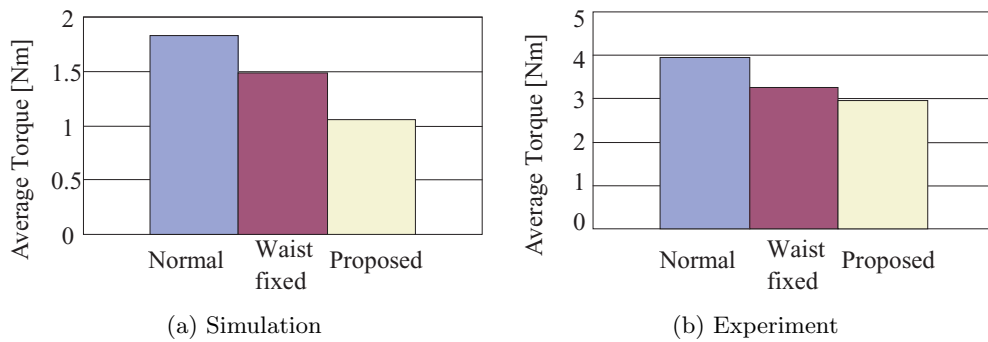


Fig. 17. Comparison of Average Torque (0.83km/h)

at 3.75km/h by the proposed walk. In other words, a 1.5 times faster walk can be realized from the view-point of the slip.

Fig.19 shows the average amplitude of the chest's fluctuation at a velocity of 1.5km/h , 2.5km/h , 3.75km/h. In the planned walking pattern, this value should ideally be zero since the upper body is always facing the forward direction. However, the upper body is rotated and fluctuated due to the slip especially in the standard walk. The proposed walk reduces this fluctuation by 40% to 50%.

Fig.20 shows the body posture of every LC at the velocity of 2.5km/h. In the original pattern, the humanoid walks straight in the forward direction. However, the slip changes the walking trajectory, especially in the standard walk. Straightness is improved by the proposed walk by reducing the slip. These results indicate the possibility that walking while using the upper body during a task can be easily accomplished.

5. Conclusion

In this paper, the trunk-twistless walk of contact sport athletes was investigated from a motion measurement. The antiphase pelvic rotation was applied to the fast walk of humanoid HRP-2. The walking action including the momentum compensation was completed only by the lower body, so that the upper body DOF can be used for accomplishing a task. Using the proposed walk, the stance foot torque and the fluctuation of the upper body were both reduced.

The investigation on fast walking in the humanoid was limited to a simulation,

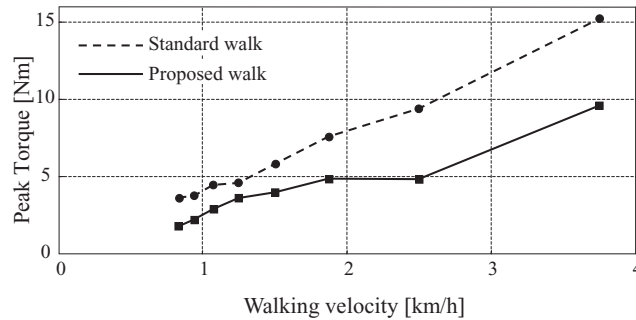


Fig. 18. Walking velocity versus Peak Torque of Stance Foot

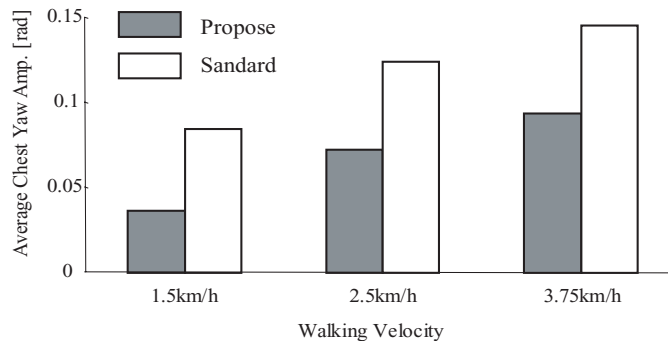


Fig. 19. Upper Body Rotation during Fast Walk (Average Yaw Amplitude)

and the applied walking velocity was not especially high when compared with human's walking velocity. A more efficient and safer hardware is required for actual experiments. The future work includes an evaluation of the energy efficiency of the trunk-twistless walk, both in humanoids and human athletes. An optimization program for an efficient walking pattern should be investigated.

The authors wish to thank Kazuhiko Hiura and Takashi Takeuchi of the Nara Institute of Science and Technology for the data processing required for this research.

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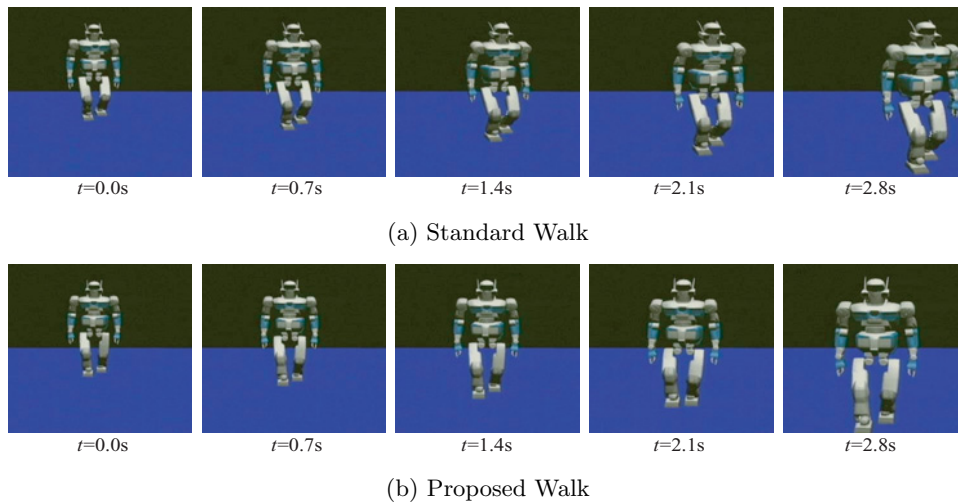


Fig. 20. Straightness of Fast Dynamic Walking (2.5km/h)

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