History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	0000	0		0000	00

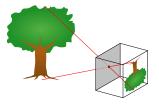
# **Event-based Computer Vision**

### Charles Clercq

#### Italian Institute of Technology Institut des Systemes Intelligents et de robotique

November 30, 2011

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
●○○○○	0000	0		0000	00
Pinho	ole came	era			



### Principle

light rays from an object pass through a small hole to form an inverted image.

▲□▶ ▲□▶ ▲三▶ ▲三▶ 三三 のへで

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
○●○○○	0000	0		0000	00
Came	era obsc	ura			

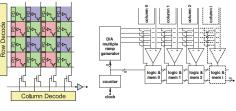


(a) 18h Century, (b) First successful perportable device for manent photograph, by artists
 Nicéphore Niépce in 1826 at Saint-Loup-de-Varennes.

### Principle

Optical device that projects an image of its surroundings on a screen.

History ○○●○○	Paradigms 0000	Event-based Computation O	Using the event-based paradigm	Validation 0000	Conclusion
Flect	ronic de	vice			

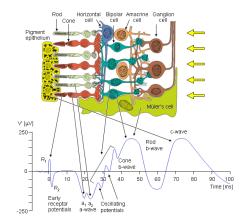


(c) CMOS sensor (d) Basic architecture of a column-parallel single-slope, multi-ramp analog-to-digital converter

### Principle

The light is integrated through the photo-diode. The value of each element is read synchronously, triggered by the time.

History ○○○●○	Paradigms 0000	Event-based Computation 0	Using the event-based paradigm	Validation 0000	Conclusion
Natu	ral "dev	vice"			



History ○○○○●	Paradigms 0000	Event-based Computation O	Using the event-based paradigm	Validation 0000	Conclusion
Visua	l systen	า			

# Principle 1

The first steps in seeing begin in the retina, where a dense array of photoreceptor convert the incoming pattern of light into an electrochemical signal [...] *Nassi, Callaway 2009* 

#### Principle 2

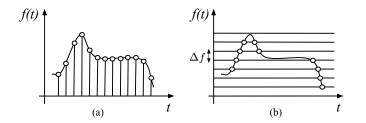
The strategy used by the mammalian visual system is to reduce the representation of the visual scene to a limited number of specialized, parallel output channels. [...] *Nassi, Callaway 2009* 

History 00000	Paradigms ●○○○	Event-based Computation O	Using the event-based paradigm	Validation 0000	Conclusion
Enco	ding				

### Two possibilities

Two ways to encode the information:

- time-driven encoding,
- data-driven encoding.



▲□▶ ▲□▶ ▲三▶ ▲三▶ 三三 のへで

History 00000	Paradigms ○●○○	Event-based Computation 0	Using the event-based paradigm	Validation 0000	Conclusion
-		Devel			

# Frame-based Paradigm

# Time-driven encoding

• fixed temporal interval, 
$$\Delta t$$
,

• 
$$I_{seq} = \{I(t_0), I(t_0 + \Delta t), \dots, I(t_0 + n\Delta t)\}$$

• 
$$I_{seq} = \{f_{0,0}(t), f_{0,1}(t), \dots, f_{M-1,N-1}(t)\}$$

 $I_{seq}$  is composed of a set of discrete functions  $f_{x,y}(t)$ , obtained by sampling all of the pixels at the same time.



History 00000	Paradigms ○○●○	Event-based Computation 0	Using the event-based paradigm	Validation 0000	Conclusion

# Frame-based issues

### Disadvantage

- Reduction of the dynamics,
- unnecessary redundant data,
- time and memory consuming.

The reason of those disadvantage come from the time sampling. To resolve the problem, we have to **change the sampling process** 

(日)、(四)、(E)、(E)、(E)

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	○○○●	0		0000	00

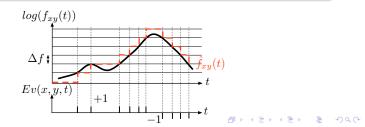
# **Event-based Paradigm**

# Sampling

• let  $t_k$  be set of times of the signal sampling,

• 
$$T = \{t_k \mid |\mathcal{F}(f_{x,y}(t_k)) - \mathcal{F}(f_{x,y}(t_{k-1}))| = \Delta f\}.$$

- ${\mathcal F}$  is defined as a log function,
  - provide a wide pixel range,
  - 2 make sensitive to the relative contrast.
- let Ev(x, y, t) be the compact representation of  $f_{x,y}$ ,
  - $Ev(x, y, t) = \delta(t, t_k) \cdot sign(f'_{x,y}(t)),$



History 00000	Paradigms 0000	Event-based Computation •	Using the event-based paradigm	Validation 0000	Conclusion 00
Com	outation				



# Goal

- exploit the data-driven acquisition advantages
- avoid the time-based issues

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	0000	O	●○○○○○○○	0000	

# **Optical Flow**

### Definition

Apparent motion of displacements in the 3D space projected on the 2D plane of image sensors

### Robotic field

The optical flow is an important tools used in the robotic field:

- object avoidance
- navigation ...



History 00000	Paradigms 0000	Event-based Computation 0	Using the event-based paradigm ○●○○○○○○	Validation 0000	Conclusion
ما حم ۱۸	a da				

### Plethora of different techniques

- differential methods,
- region-based matching,
- energy based,

methods

• phased based.

#### Two distinct families

- Purely local (e.g Lucas and Kanade),
- Global (e.g Horn and Schunck),
  - take advantage of the global image structure.

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	0000	0		0000	00

# Selection

#### Local method

Taking advantage of:

- high temporal resolution,
- sparse encoding.

# Small displacement and assumption

• The light intensity conservation

• 
$$I(x, y, t) = I(x + \delta x, y + \delta y, t + \delta t)$$

Taylor series

•  $I(x+\delta x, y+\delta y, t+\delta t) = I(x, y, t) + \frac{\partial I}{\partial x}\delta x + \frac{\partial I}{\partial y}\delta y + \frac{\partial I}{\partial t}\delta t + H.O.T$ 

• The equation of the optical flow

• 
$$I_x V_x + I_y V_y = -I_t$$

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	0000	0	○○○●○○○○	0000	
Least	Square	e Method			

### Estimation

 Local constancy •  $\begin{cases} I_x(q_1)V_x + I_y(q_1)V_y = -I_t(q_1) \\ \dots \\ I_y(q_n)V_x + I_y(q_n)V_y = -I_t(q_n) \end{cases},$  The Least Square Method •  $A = \begin{bmatrix} I_x(q_1) & I_y(q_1) \\ I_x(q_2) & I_y(q_2) \\ \vdots & \vdots \\ I_x(q_n) & I_y(q_n) \end{bmatrix}, v = \begin{bmatrix} V_x \\ V_y \end{bmatrix}, b = \begin{bmatrix} -I_t(q_1) \\ -I_t(q_2) \\ \vdots \\ -I_t(q_n) \end{bmatrix}.$ •  $A^T A v = A^T h$ 

• To solve:

• 
$$v = (A^T A)^{-1} A^T b$$

History	Paradigms	Event-based	Computation

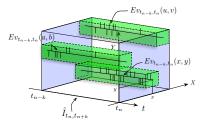
Using the event-based paradigm

Validation 0000 Conclusion 00

# **Event-based** Optical Flow

# Derivative

$$\begin{cases} \frac{\partial l_{t_i,t_n}}{\partial x}(x,y) &\sim (Ev_{t_i,t_n}(x,y) - Ev_{t_i,t_n}(x-1,y))\Delta f\\ \frac{\partial \hat{l}_{t_i,t_n}}{\partial y}(x,y) &\sim (Ev_{t_i,t_n}(x,y) - Ev_{t_i,t_n}(x,y-1))\Delta f\\ \frac{\partial \hat{l}_{t_i,t_n}}{\partial t}(x,y) &\sim \frac{Ev_{t_i,t_n}(x,y) - Ev_{t_i,t_{n-k}}(x,y)}{t_n - t_{n-k}}\Delta f \end{cases}$$



◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

History 00000	Paradigms 0000	Event-based Computation O	Using the event-based paradigm	Conclusion

# Optical Flow Algorithm

#### Algorithm: Event-based optical flow

**Require:** 
$$\mathbf{p} = [x, y]^t$$

For each event occurring at time t at pixel  $[x, y]^t$ : Define a  $(n \times n)$  neighborhood N of  $[x, y]^t$  and compute the

partial derivatives:

• 
$$grad(I)(\mathbf{p}) = \begin{bmatrix} \frac{\partial \hat{l}_{t_j,t_n}}{\partial x}(\mathbf{p}) \\ \frac{\partial \hat{l}_{t_j,t_n}}{\partial y}(\mathbf{p}) \end{bmatrix}$$
  
•  $\frac{\partial I}{\partial t}(\mathbf{p}) = \frac{Ev_{t_{n-k},t_n}}{t_n - t_{n-k}} \Delta f$ 

Solve equation of the flow over  $\mathbb{N}$  for  $[v_x, v_y]^t$ 

Paradigms Event-based Computation

00000000

Using the event-based paradigm

Validation

Conclusion

# Optical Flow Algorithm and noise

Algorithm: Event-based optical flow 2

**Require:**  $\mathbf{p} = [x, y]^t$ 

е

For each event occurring at time t at pixel  $[x, y]^t$ :

if activity  $Act_{t_n-k,t_n}(x,y) > a$  then Define a  $(n \times n)$  neighborhood N of  $[x, y]^t$  and compute the partial derivatives:

• 
$$grad(I)(\mathbf{p}) = \begin{bmatrix} \frac{\partial \hat{l}_{t_j,t_n}}{\partial x}(\mathbf{p}) \\ \frac{\partial \hat{l}_{t_j,t_n}}{\partial y}(\mathbf{p}) \end{bmatrix}$$
  
•  $\frac{\partial I}{\partial y}(\mathbf{p}) = \frac{Ev_{t_{n-k},t_n}}{\Delta f} \Delta f$ 

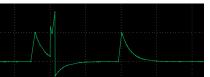
$$\frac{\partial I}{\partial t}(\mathbf{p}) = \frac{L v_{t_{n-k},t_n}}{t_n - t_{n-k}} \Delta$$

Solve equation of the flow over  $\mathbb{N}$  for  $[v_x, v_y]^t$ else

set 
$$v_x = 0$$
 and  $v_y = 0$   
nd if

History 00000	Paradigms 0000	Event-based Computation 0	Using the event-based paradigm ○○○○○○○●	Validation 0000	Conclusion		
Noise	e issue						
Si	mple filte	r					
Ν		ive on the events					
	<ul> <li>Accumulation and inhibition:</li> <li>leaky integration over Δt,</li> <li>comparison to a threshold,</li> <li>hyper-polarization.</li> </ul>						
	- · ·	endent on stimulu eters should be va					

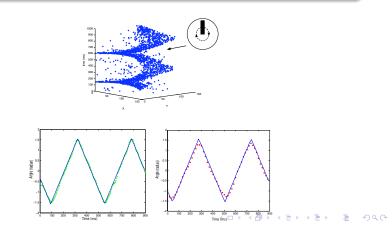




History 00000	Paradigms 0000	Event-based Computation 0	Using the event-based paradigm	Validation ●○○○	Conclusion
Orier	ntation				

### Protocol

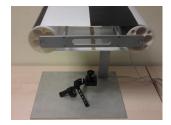
Use of a black bar painted on a white disk, rotating with a constant angular velocity

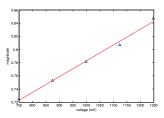


History 00000	Paradigms 0000	Event-based Computation O	Using the event-based paradigm	Validation ○●○○	Conclusion
Amp	litude				

#### Protocol

Use of a moving pattern of bars whose translational speed can be accurately set by adjusting the supply voltage of a DC motor.

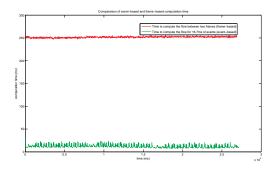




History 00000	Paradigms 0000	Event-based Computation 0	Using the event-based paradigm	Validation ○○●○	Conclusion
Com	putatior	nal cost			

# Protocol

Comparison of the computational times required by the frame-based and the event-based methods for computing optic flow



▲□▶ ▲□▶ ▲臣▶ ★臣▶ 三臣 - のへで

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	0000	O		○○○●	00
Com	outation	al cost			

### Comparison

- frame-based, 60 fps (16.7 ms)
  - number of processed pixels at each step: 16384,
  - mean computation time: 251.7ms

### mean computation of a pixel: $15.4e^{-3}ms$

- event-based  $(1e^{-3}ms)$ 
  - mean number of events (period of 16.7ms): 1340,

▲□▶ ▲□▶ ▲□▶ ▲□▶ ▲□ ● ● ●

• mean computation time: 9.65ms

# mean computation of an event: $7.2e^{-3}ms$

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	0000	0		0000	●○
Conc	lusion				

### The data-driven, bioinspired sampling

- removes redundancies,
- better captures the dynamic content of visual input.

### event-based optical flow

The experiments showed that the new asynchronous event-based paradigm allows for

- high dynamic computation
- fast and low cost computation

History	Paradigms	Event-based Computation	Using the event-based paradigm	Validation	Conclusion
00000	0000	0		0000	○●
Disci	ission				

#### Further works

The method is sensible to noise, to deal with different method are explored:

- short term depression in input synapses,
- spike frequency adaptation of the leaky integration.